



Comparison of Heat Transfer Performance of Lattice-Structured Heat Sinks

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ABSTRACT

This paper presents a comparative study of the heat transfer performance of lattice-structured heat sinks. Twenty different unit cells are chosen, and heat sinks are modeled in nTop with constant unit cell size. Al 6061 alloy is chosen as the material for analysis due to its good thermal conductivity, low weight, low cost, and high strength. Steady-state thermal analysis is performed using ANSYS with constant input parameters for all samples. Heat flux and temperature distribution within the heat sinks are analyzed. From the simulation, it was found that TPMS and plate-based heat sinks outperform other types with better heat transfer.

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1. INTRODUCTION

Efficient heat transfer is crucial in various engineering applications, ranging from electronics cooling to HVAC systems, where enhancing heat dissipation capabilities can significantly improve system performance and reliability. Numerous studies have investigated the influence of fin geometry, such as shape (Arefin, 2016; Kushwaha et al., 2013), size, arrangement (Shah, 2016), and spacing (Yardi et al., 2017; Dewan et al., 2010), on heat transfer performance. Advancements in manufacturing techniques have enabled the fabrication of intricate fin designs to enhance heat transfer efficiency further (Catchpole-

Smith et al., 2019). Lattice structures, drawing inspiration from the intricate patterns found in nature's cellular formations (Nazir et al., 2019), have been designed to overcome inherent fin shape and structure limitations. Lattice structures, characterized by their periodic arrangement of unit cells, possess distinct advantages such as high surface area-to-volume ratio, high strength-to-weight ratio (Perween et al., 2021), and low relative density. These attributes make lattice heat sinks promising candidates for efficient heat dissipation applications. However, comprehensive analyzes evaluating the thermal

performance analyzes evaluating the thermal performance of lattice heat sink designs remain limited. This paper presents a systematic investigation into the heat transfer characteristics of heat sinks with lattice structures using numerical analysis.

2. LATTICE STRUCTURES

Lattice structures, also known as architected cellular materials, are a type of cellular structure with repeating unit cells (Dong et al., 2017). Certain physical properties of lattice structures can be tailored by controlling their geometrical parameters (Schaedler & Carter, 2016). Some lattice structures, e.g., lattice metamaterials, exhibit unique characteristics (Talebi et al., 2021) such as negative Poisson ratio (Bhate & Hayduke, 2023), negative compressibility, negative thermal expansion, phononic band gap, etc., which make them useful for a wide range of applications, including light-weighting, energy absorption, bio-scaffolds, noise/vibration wave insulation,

and thermal management (Jia et al., 2020). Lattice structures have been found to break the parasitic performance trade-offs (Jia et al., 2019) seen in bulk materials such as strength vs. toughness (Ritchie, 2011; Bouville et al., 2014), stiffness vs. energy dissipation, flexibility vs. fast response, etc. The lattice structures' high surface area to volume ratio makes them an ideal choice for high-performance heat exchanger applications. Powered by the rapid development of additive manufacturing techniques, compact lattice heat sinks may soon replace traditional heat sink types.

Based on the type and arrangement of unit cells, lattice structures are grouped into many classes (Benedetti et al., 2021; Pei et al., 2022; Abou-Ali et al., 2022; Guo et al., 2019; Tancogne-Dejean et al., 2018; Andrew et al., 2021; Pronk et al., 2017; McGregor et al., 2021; Tyagi et al., 2023; Andrei et al., 2021) as shown in **Figure 1** (unit cell-based) and **Figure 2** (periodicity-based).

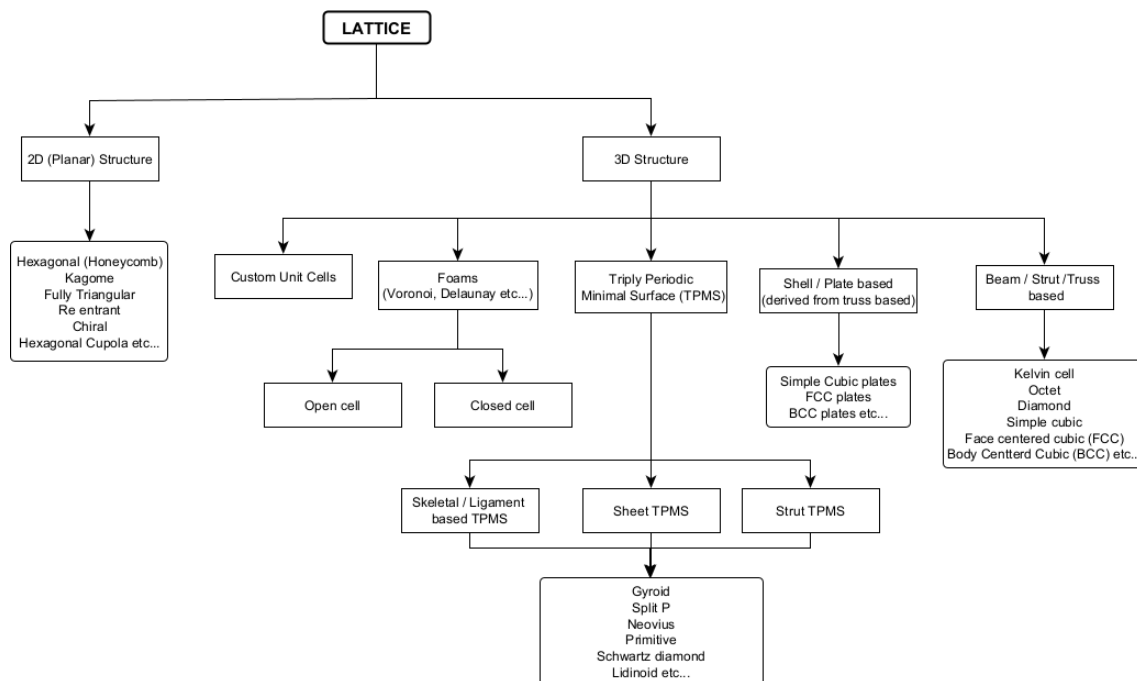


Figure 1. Classification of lattice structures based on unit cell

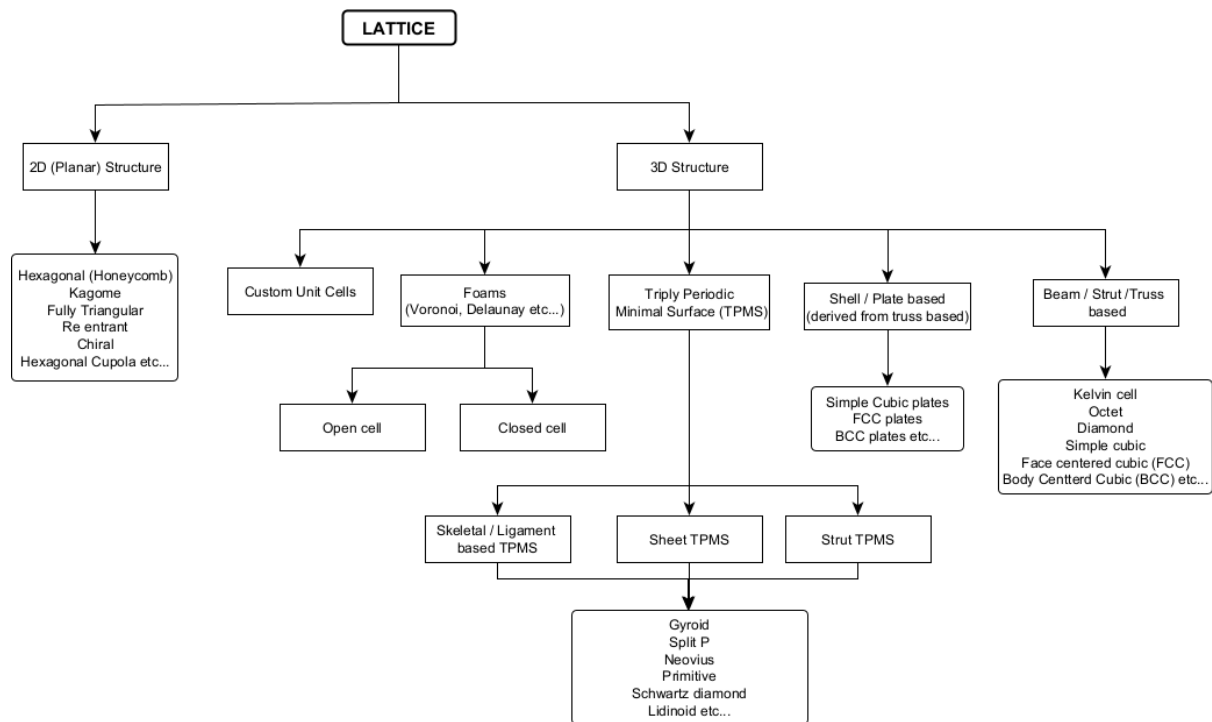


Figure 2. Classification of lattice structures based on periodicity

3. METHODOLOGY

3.1. Geometric Modelling

The fins are modeled using nTop, an implicit modeling software. Unlike explicit modeling techniques, which represent a body as a set of polygons or parametric patches (Opalach & Maddock, 1995), implicit modeling technique distinguishes between points inside and outside a body by representing them as a function or scalar field (Fayolle et al., 2017). This allows for creating complex shapes and features that are otherwise impossible to model with explicit modeling software. Implicit modeling is also ideal for designing additively manufactured parts. However, implicit models

require significantly high computational resources and are not the ideal method to represent 3d models for subtractive manufacturing, as calculating the boundary of the slice is a complicated process (Li et al., 2018). All fins taken for analysis possess similar basic dimensions, shown in **Figure 3**. The unit cells selected for analysis are depicted in **Figure 4**, **Figure 5**, and **Figure 6**. Constant unit cell sizes are used throughout the analysis. The unit cells chosen for analysis are shown in **Figure 4** for beam/truss-based unit cells, **Figure 5** for 2D and plate-based unit cells, and **Figure 6** for triply periodic minimal surface (TPMS) unit cells. All unit cells are of the following dimensions: 15mm x 20mm x 20mm.

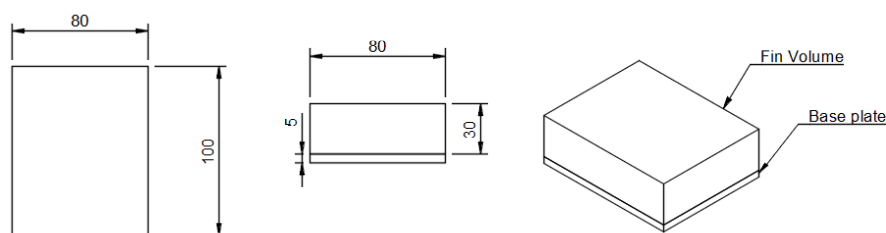


Figure 3. Basic heat sink dimensions

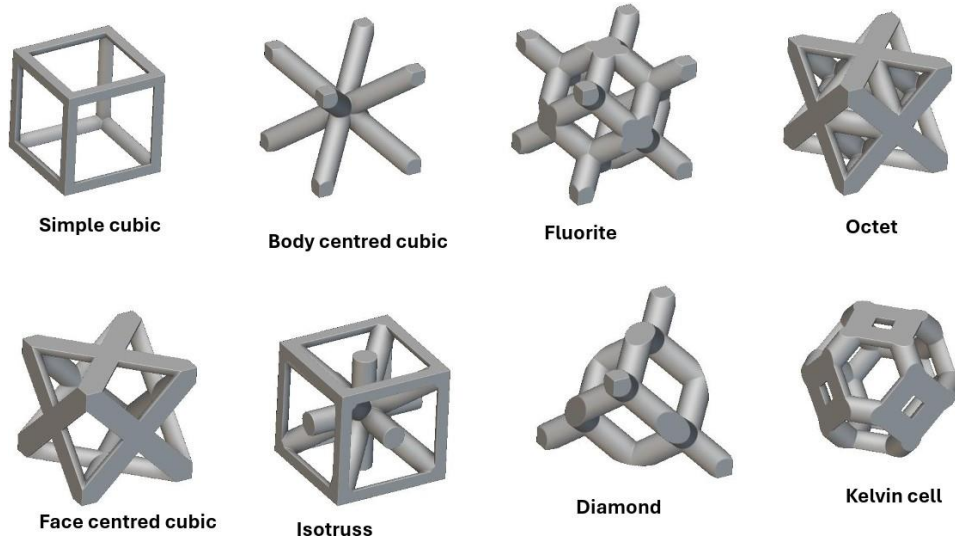


Figure 4. Beam/Truss-based unit cells.

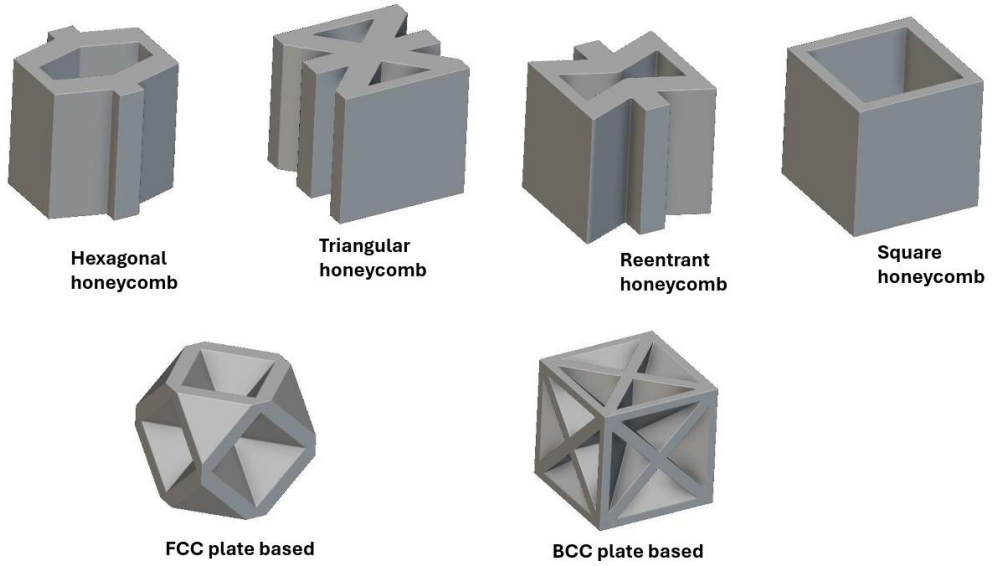


Figure 5. 2D and plate-based unit cells.

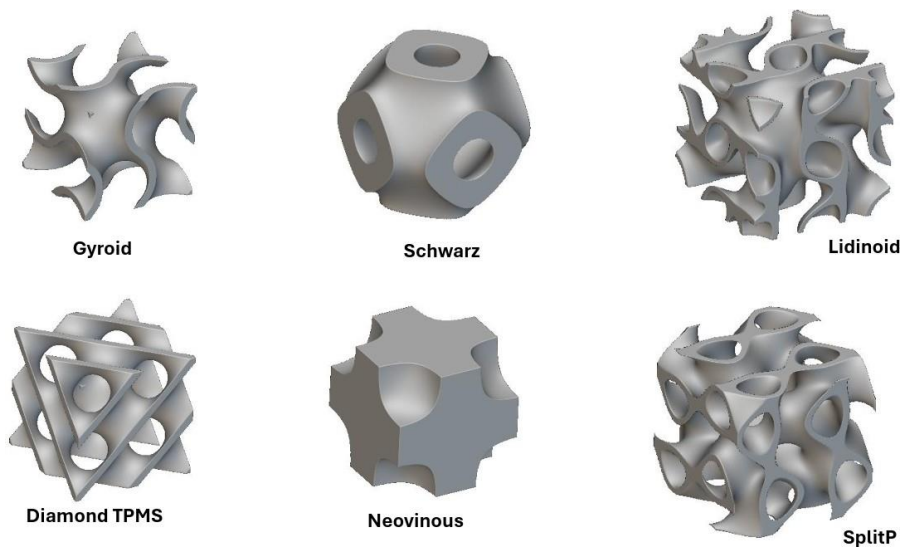


Figure 6. TPMS unit cells

3.2. Finite Element Analysis

The steady-state thermal analysis is carried out using ANSYS. In steady-state analysis, the object under study is assumed to be in equilibrium, and ambient conditions are also assumed to be constant. The same material properties and boundary conditions are defined for all heat sink types. The material is assumed to be isotropic and homogeneous with constant thermal conductivity.

3.2.1. Material Properties

Aluminium alloys are typically preferred for heat sinks due to their excellent thermal conductivity, low weight, low cost, and high strength. Al 6000 series alloys are widely used as they can be extruded easily. Al 6061 alloy is taken for analysis. Some essential properties of Al 6061 alloy are given below:

- Material: Al 6061 T6
- Density: 2713 kg/m³
- Poisson's Ratio: 0.33
- Young's modulus: 6.904E+10 Pa
- Bulk modulus: 6.7686E+10 Pa
- Isotropic Thermal Conductivity: 155.3 W/m.K
- Ultimate Tensile strength: 3.131E+8 Pa
- Specific Heat (constant Pressure): 915.7 J/kg.K
- Isotropic Secant Coefficient of Thermal Expansion: 2.278E-5 /K
- Composition of Al 6061 alloy is shown in **Table 1**.

Table 1. Material composition (Al 6061).

Element	Wt. %
Al	95.898.6
Cr	0.040.35
Cu	0.150.4
Fe	Max 0.7
Mg	0.81.2
Mn	Max 0.15
Si	0.40.8
Ti	Max 0.15
Zn	Max 0.25

3.2.2. Boundary Conditions

In this study, a constant film coefficient is assumed for simplicity. In actual practice, the film coefficient of a heat sink depends on various factors, such as surface roughness, geometrical parameters, fluid properties (viscosity, density), flow rate, heat flux, temperature gradient, etc. (Moreira et al., 2019). Additionally, obtaining an accurate value of the heat transfer coefficient is difficult as it changes locally and temporally (Grądział et al., 2019; Bury & Hanuszkiewicz-Drapala, 2018; Erdoğan, 2008; D. V. Abramkina et al., 2018; Korprasertsak & Leephakpreeda, 2017). Heat transfer due to radiation is neglected. A constant heat input of 100W is given in the bottom face of the base plate (**Figure 7(a)**) and convection boundary conditions is applied in the sample (**Figure 7(b)**).

The following boundary conditions are defined, as follows: Film coefficient is 25 W/m² K, heat flow(base) is 100 W, and ambient temperature is 30⁰ C. The heat sink data is shown in **Table 2** and mass vs surface area plot is shown in **Figure 8**.

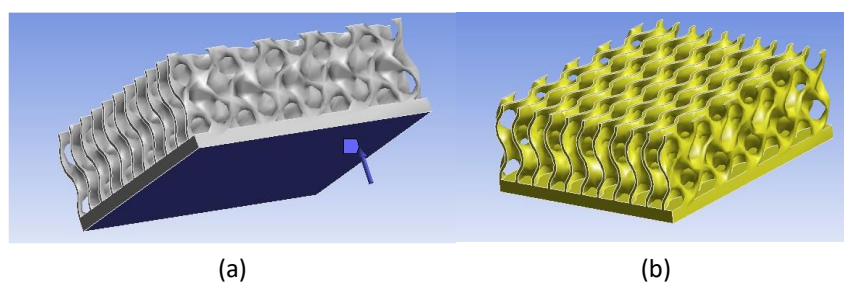


Figure 7(a). Heat flow (input) boundary (b). Convection boundary

Table 2. Heat Sink Data

Unit cell type	Thickness (mm)	Nodes	Elements	Mass(g)	Surface area (mm ²)	Wt. %
Simple cubic	4	223143	138108	173.74	44571.33	22.87136012
Body centered cubic	3	279253	162839	191.86	55570.87	25.25670054
Face centered cubic	3	321148	187137	208.27	66091.82	27.41693434
Diamond	3	304447	181469	191.64	55724.85	25.22773946
Octet	3	526883	316205	291.18	98070.46	38.33131483
Kelvin cell	3	303670	177447	206.2	62850.66	27.14443684
Fluorite	3	438067	258296	260.78	82638.74	34.3294192
Isotruss	3	219156	136626	253.29	81405.53	33.34342583
Triangular honeycomb	3	343357	224716	494.2	96459.57	65.05713233
Hexagonal honeycomb	3	29284	122089	355	74245.7	46.73266284
Reentrant honeycomb	3	219977	135062	417.63	87043.11	54.9773577
Square honeycomb	3	123582	74924	289.2	60256.69	38.07066505
FCC plate	1	428251	253213	326.36	155390.4	42.9624559
BCC plate	1	477545	296874	370.86	180576.59	48.82049392
Gyroid	2	197347	103200	247.82	102846.45	32.6233479
Schwarz	2	207814	121741	350.62	79234.29	46.15607393
Diamond TPMS	2	226259	116393	275.64	120721.57	36.28560897
Lidinoid	2	281184	166176	360.86	157632.11	47.50408088
SplitP	2	609100	325740	295.65	152601.96	38.91975146
Neovinous	1	866475	597273	422.76	74812.35	55.65267758

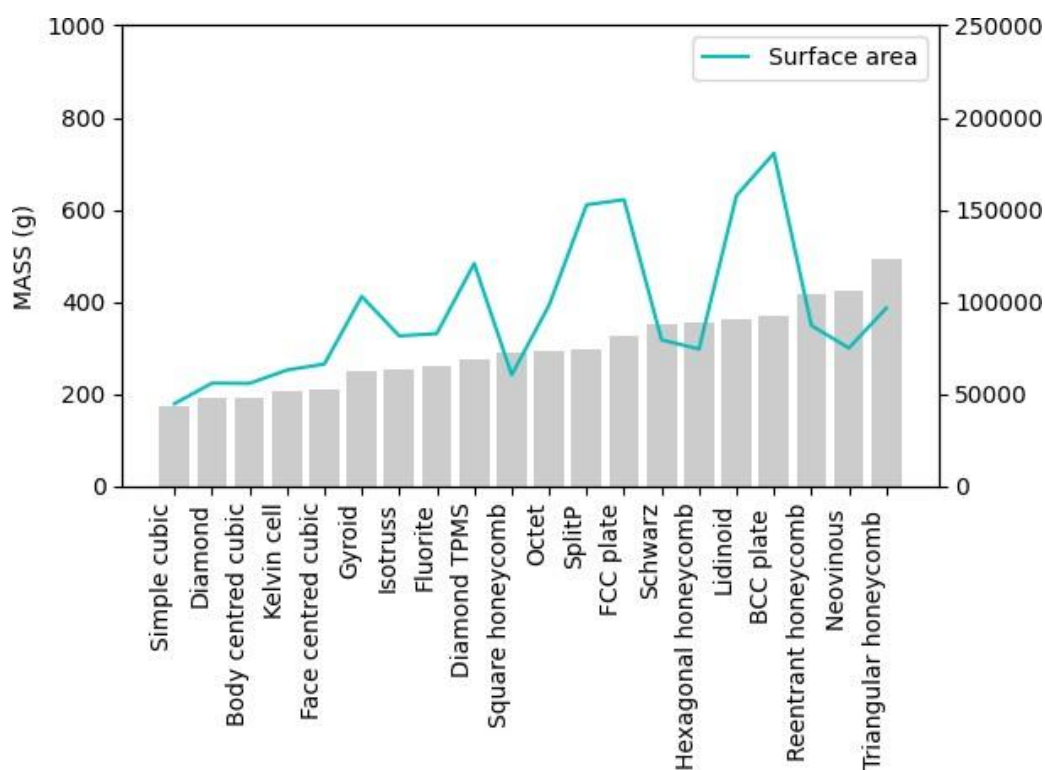


Figure 8. Mass vs Surface area plot

4. RESULTS AND DISCUSSION

Table 3 shows the values of temperature and heat flux from the simulation. The highest temperature difference within the simple cubic heat sink. However, the maximum temperature produced in the simple cubic heat sink is the highest among all types taken for analysis, which may limit its practical applications. The maximum temperature reached in plate-based heat sinks is lower than in other types. In most cases, the temperature difference increases with the decreasing mass of the heat sink with the same film coefficient (Figure 9).

Figure 10 show the temperature distribution in the various unit cell. Temperature distribution in the 2D lattice structured heat sinks is not uniform along the vertical axis and changes based on the unit cell orientation. Figure 11 show the heat flux distribution of the various unit cell

type. A more uniform heat flux distribution is seen in 2D, honeycomb, and TPMS lattices than in beam/truss-based structures.

Figure 12 shows the minimum and maximum temperature for the various unit cell. It can be seen that the simple cubic has the highest maximum temperature. In addition, the simple cubic has also the highest heat flux (Figure 13). Mass and temperature difference plot is shown in Figure 14. Temperature difference against surface area plot is shown in Figure 15. The results are highly subject to the design parameters of unit cells and the heat transfer coefficient. For a given value of film coefficient, beam/truss-based heat sinks outperform other types in terms of mass and temperature difference produced. Future works may analyze the heat transfer properties of heat sinks with film coefficient obtained using computational fluid dynamic (CFD) analysis results.

Table 3. Analysis results of various unit cell types

Unit cell type	Min. temp. (°C)	Max. temp. (°C)	Temperature difference (°C)	Min heat flux (W/m ²)	Max. heat flux (W/m ²)
Simple cubic	104.16	176.89	72.73	365.95	5.61E+05
Body centered cubic	89.87	144.43	54.56	99.05	4.82E+05
Face centered cubic	75.89	128.43	52.54	171.42	2.43E+05
Diamond	86.84	144.33	57.49	41.645	4.31E+05
Octet	64.18	90.85	26.67	41.633	1.34E+05
Kelvin cell	83.23	129.14	45.91	175.63	4.17E+05
Fluorite	71.93	101.24	29.31	56.76	3.00E+05
Isotruss	69.61	104.44	34.83	135.36	2.29E+05
Triangular honeycomb	72.54	80.04	7.5	572.32	50991
Hexagonal honeycomb	85.58	95.22	9.64	246.49	1.29E+05
Reentrant honeycomb	76.86	86.59	9.73	195.95	99972
Square honeycomb	104.63	109.75	5.12	654.98	69641
FCC plate	52.44	66.94	14.5	143.12	99131
BCC plate	49.34	61.32	11.98	53.9	1.00E+05
Gyroid	64.4	84.07	19.67	149.76	1.23E+05
Schwarz	80.96	93.69	12.73	219.91	1.44E+05
Diamond TPMS	58.67	74.94	16.27	107.53	1.57E+05
Lidinoïd	66.23	76.42	10.19	135.47	64755
SplitP	51.46	66.83	15.37	67.57	1.82E+05
Neovinous	86.51	95.77	9.26	129.53	72583

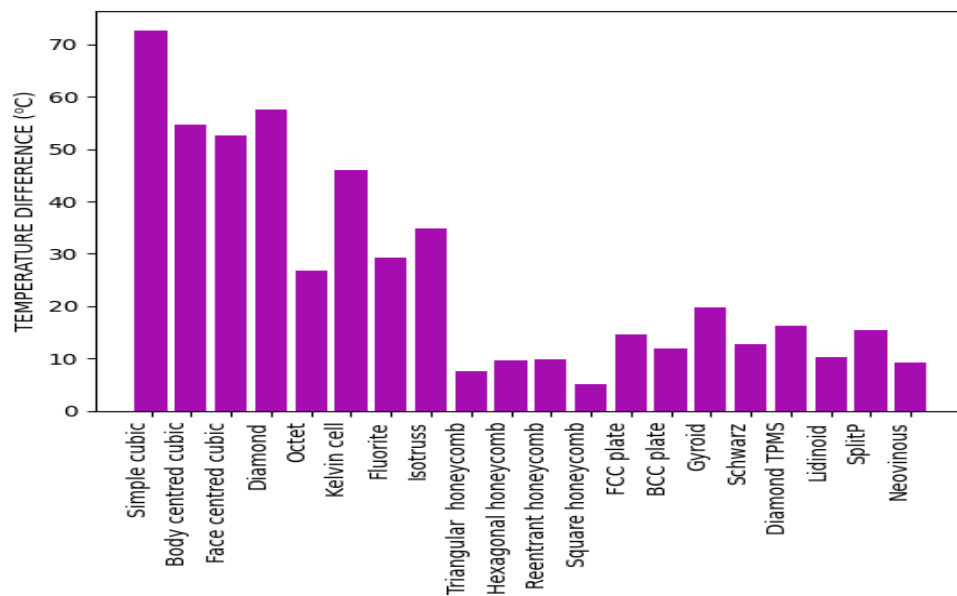
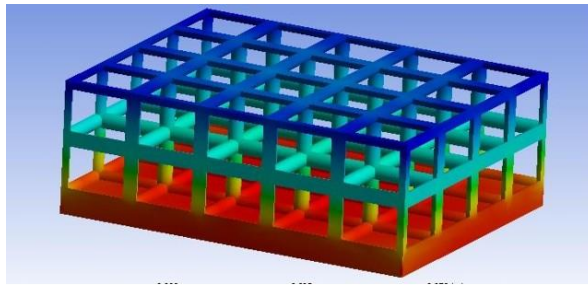
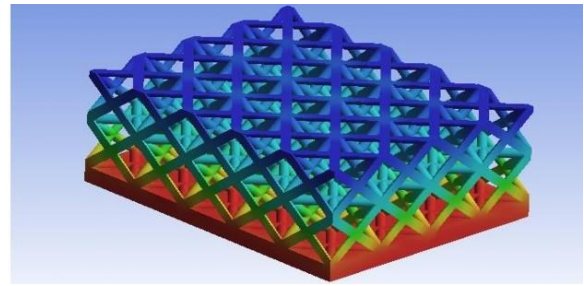


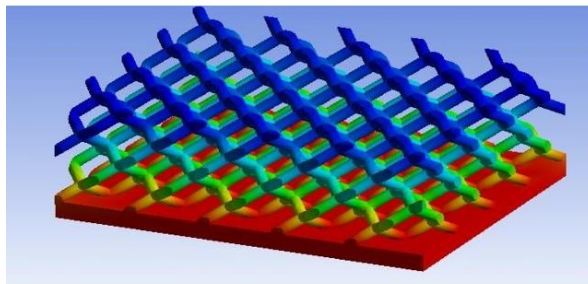
Figure 9. Temperature difference



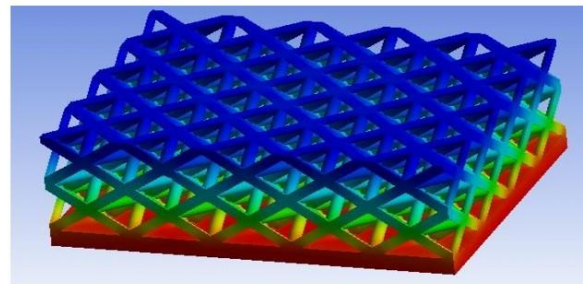
Simple cubic



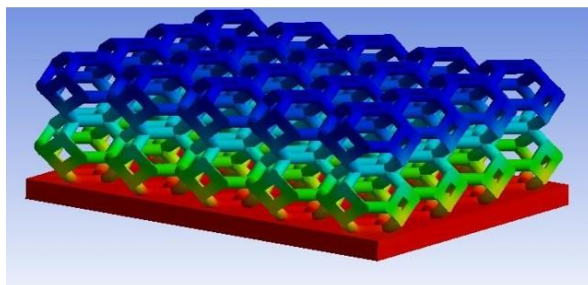
Face centred cubic



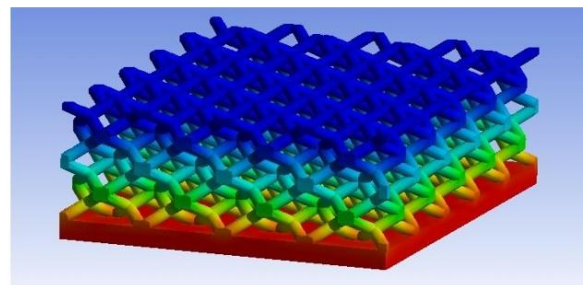
Diamond



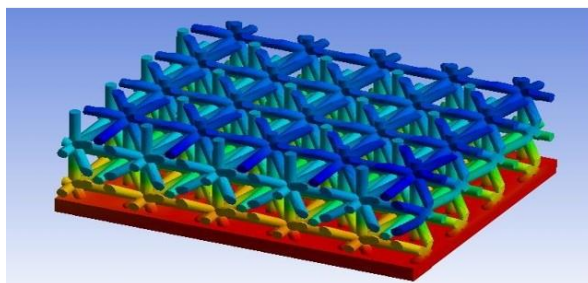
Octet



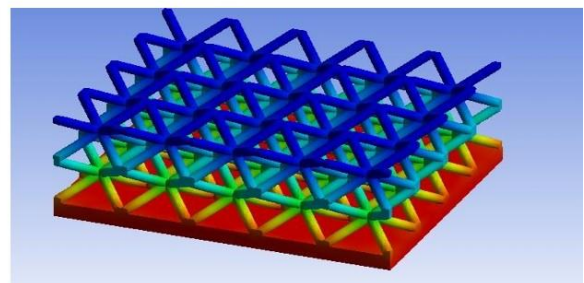
Kelvin cell



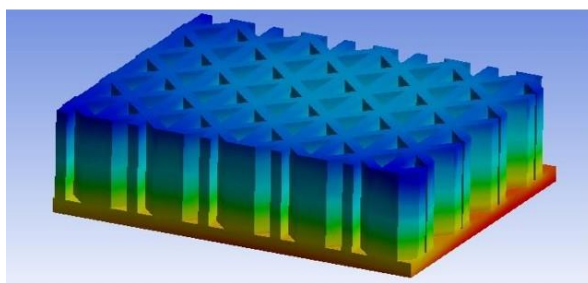
Fluorite



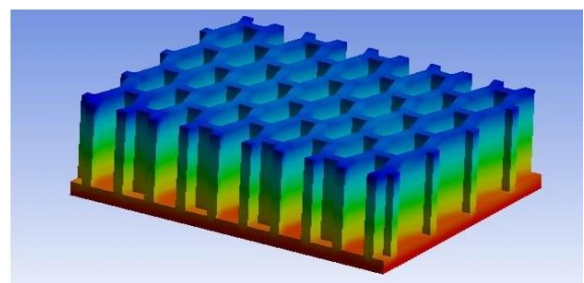
Isotruss



Body centred cubic

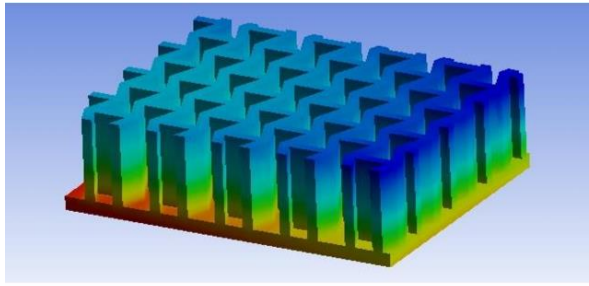


Triangular honeycomb

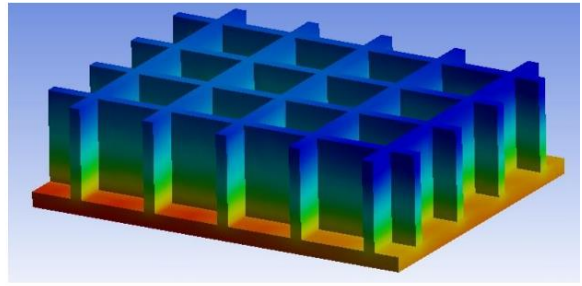


Hexagonal honeycomb

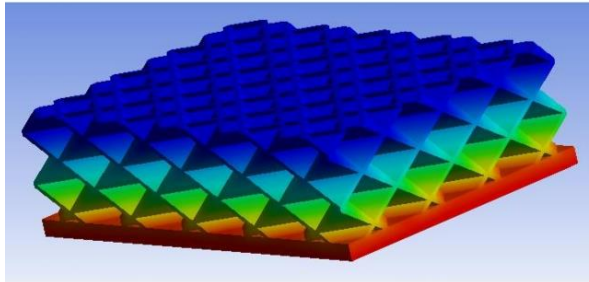
Figure 10. Temperature distribution results



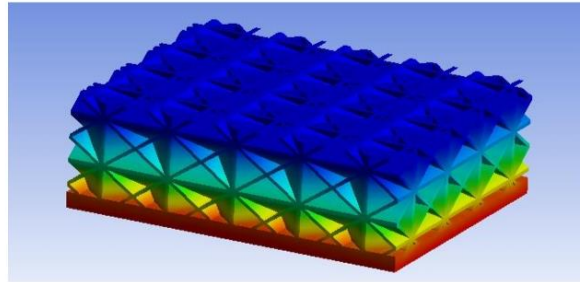
Reentrant honeycomb



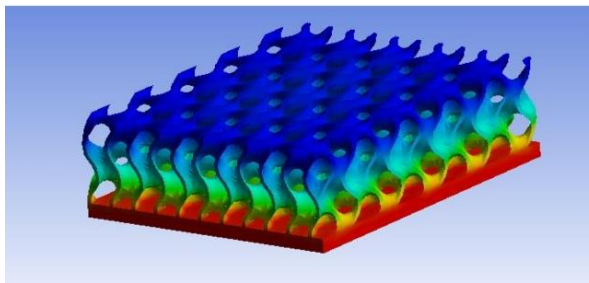
Square honeycomb



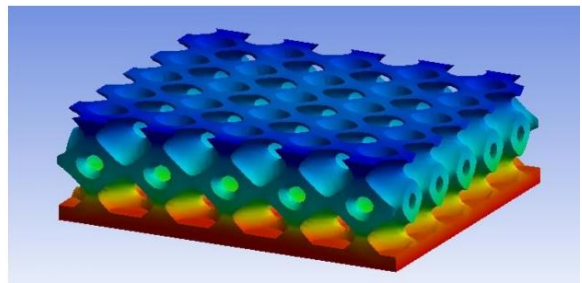
FCC (plate based)



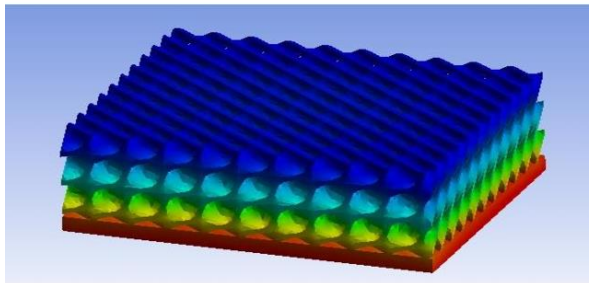
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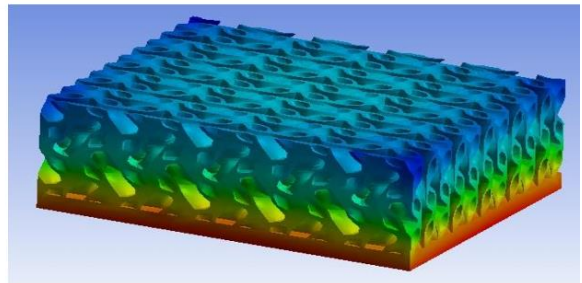
Gyroid



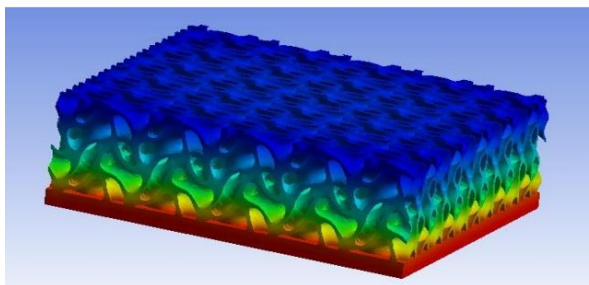
Schwarz



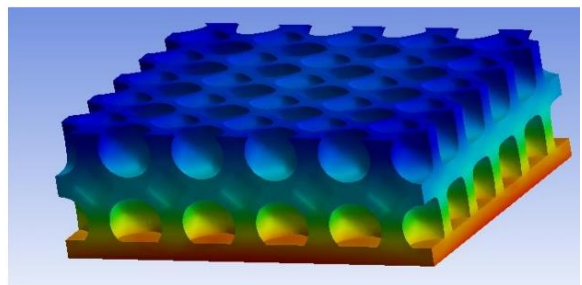
Diamond TPMS



Lidinoid



splitP



Neovinous

Figure 10. Temperature distribution results (continued)

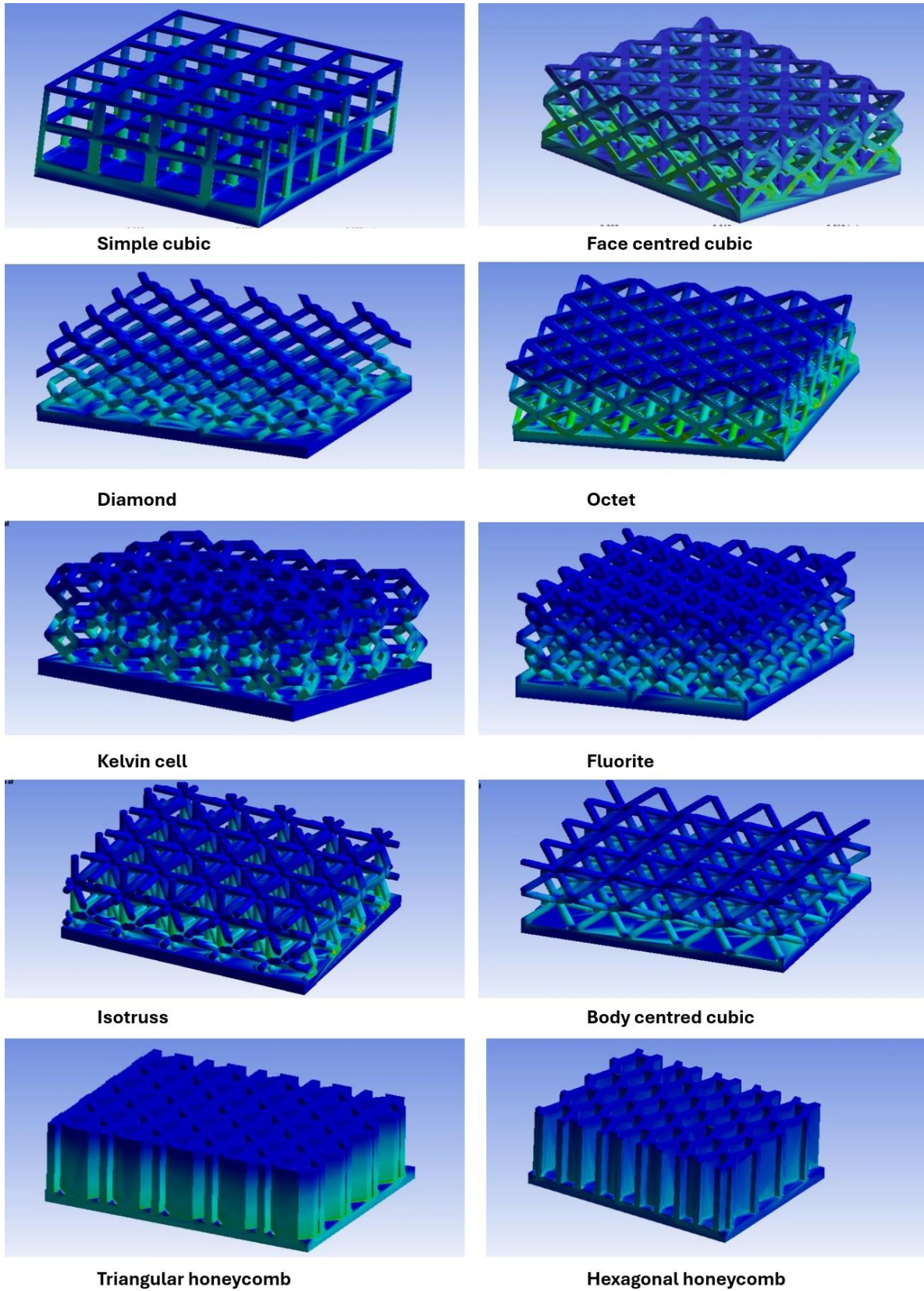
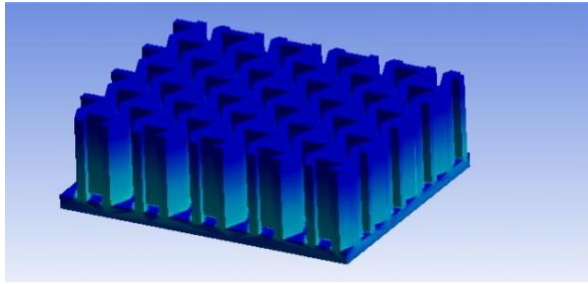
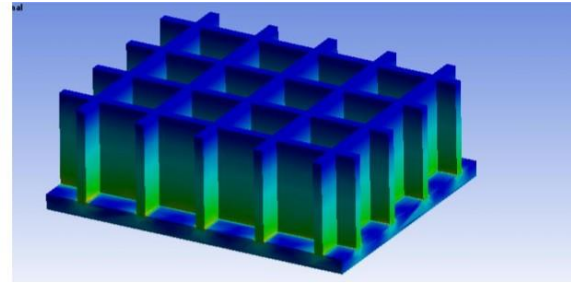


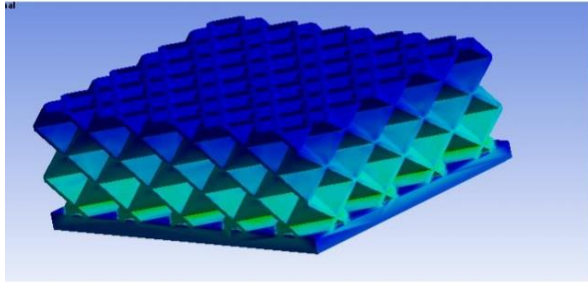
Figure 11. Heat flux distribution



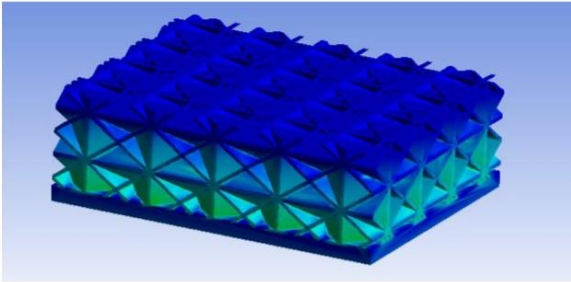
Reentrant honeycomb



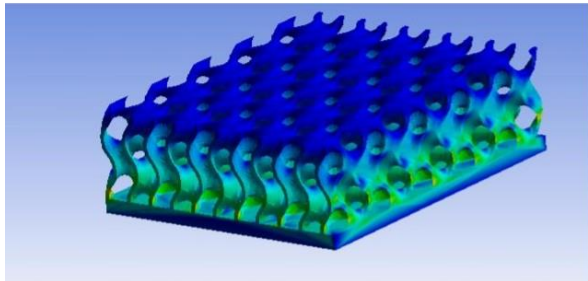
Square honeycomb



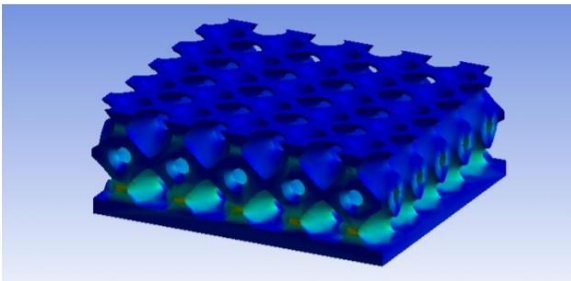
FCC (plate based)



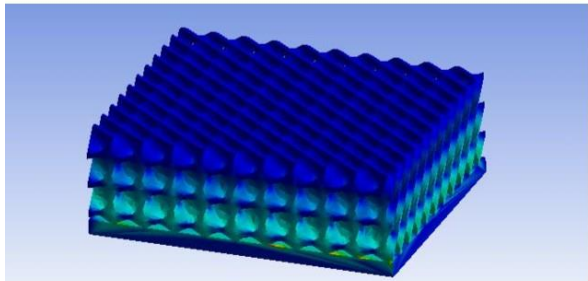
BCC (plate based)



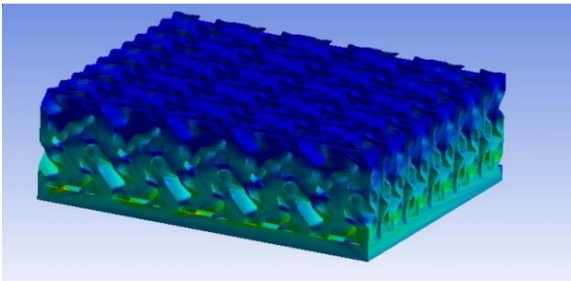
Gyroid



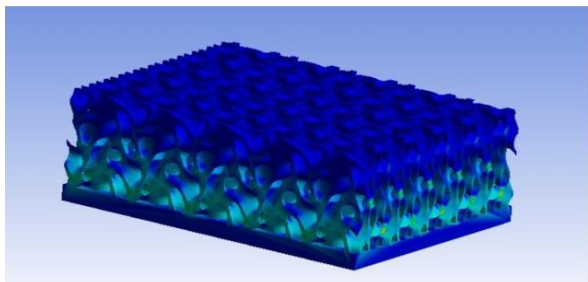
Schwarz



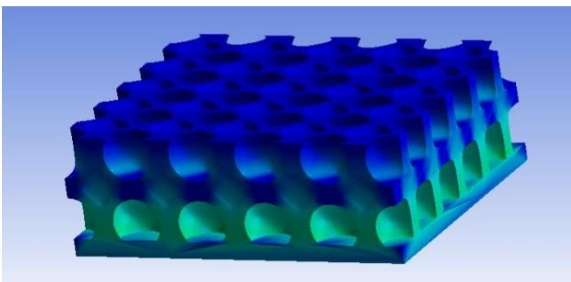
Diamond TPMS



Lidinoid



splitP



Neovinous

Figure 11. Heat flux distribution (continued)

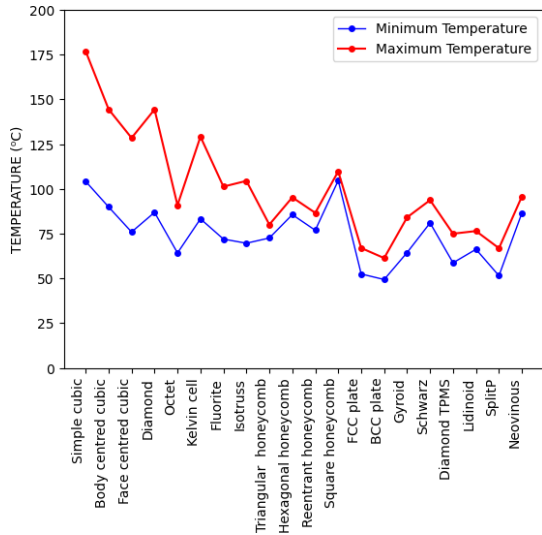


Figure 12. Minimum and maximum temperatures plot

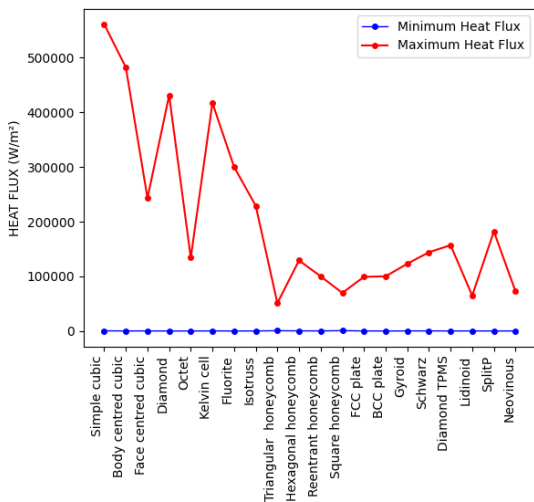


Figure 13. Minimum and maximum heat flux plot

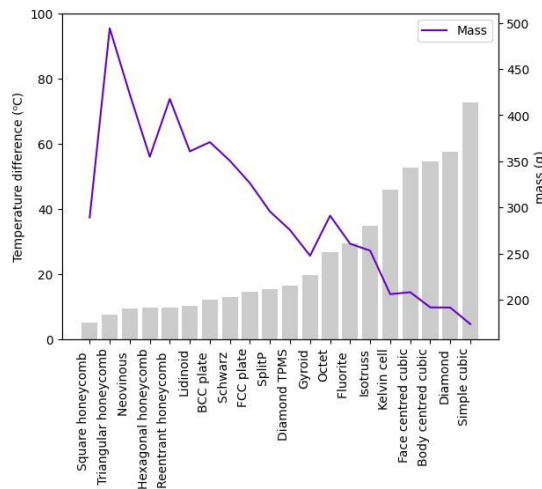


Figure 14. Mass vs Temperature difference plot

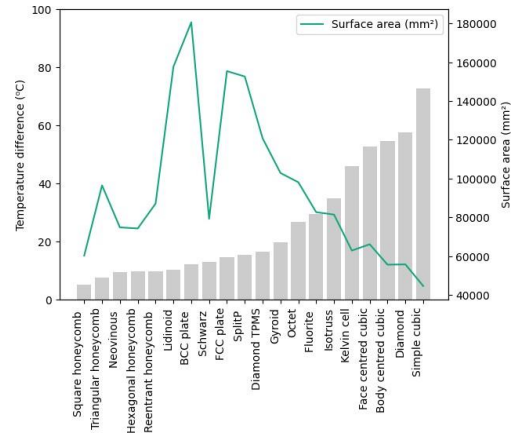


Figure 15. Temperature difference vs surface area plot

5. CONCLUSION

Various unit cell has been tested in order to identify their performance in heat transfer process. The steady state thermal analysis using ANSYS simulation is conducted. The results interpret that TPMS, and plate-based heat sinks have better overall performance due to their higher surface area and more significant temperature gradient. They also possess a low mass density.

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